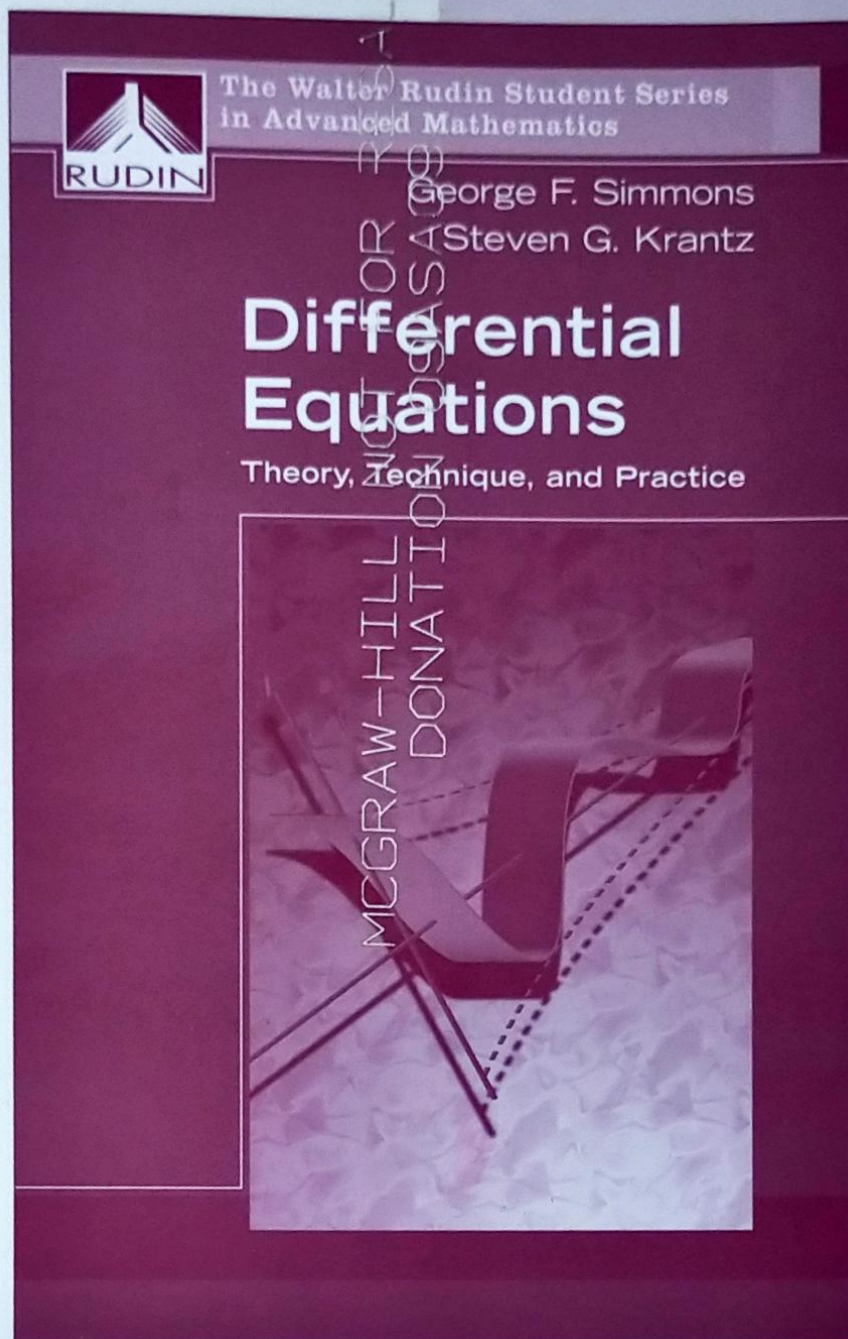


Student's Solutions Manual

to accompany



Prepared by
Donald Hartig

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to accompany

Differential Equations

Theory, Technique, and Practice

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Student's Solutions Manual to accompany
DIFFERENTIAL EQUATIONS: THEORY, TECHNIQUE, AND PRACTICE
GEORGE F. SIMMONS AND STEVEN G. KRANTZ

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